

3:30 pm

PHD

Net
hate
M hat

Graph Theory

COMPLETE REVISION

Daily live class at 3:30pm



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Rashmi Prabha
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next week

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Pause
2 concept

Q1) Let G be a complete undirected graph on 6 vertices. If vertices of G are labeled, then no. of distinct cycle of length 4 in G is equal to ...? (Gate 2012)

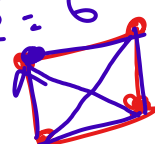
- A. 15
- B. 30
- C. 90
- D. 360

$$\frac{n(n-1)}{2}$$
$$= \frac{6 \times 5}{2} = 15$$

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$n=4$
 $e=6$


Complete Undirected
 Regular Graph \rightarrow nodes
 complete graph? $deg = same$
wrong
 \hookrightarrow nodes adjacent
 Total no. of max edges
 $\frac{n \cdot (n-1)}{2}$

Q1) Let G be a complete undirected graph on 6 vertices. If vertices of G are labeled, then no. of distinct cycle of length 4 in G is equal to ...? (Gate 2012)

- A. 15
- B. 30
- C. 90
- D. 360

Complete Graph
 \checkmark No. of edges = $\frac{n(n-1)}{2}$
 \checkmark Distinct cycle length = $(n-1)! = (4-1)! = 3!$
 $15 \cdot 3! = 90$
 = regular complete
 loop
 yes
 No

pass

applicative

Q2) What is the chromatic number of n vertex simple connected graph which does not contain any odd length cycle. Assume $n \geq 2$.

- a) N
- b) N-1
- c) 2
- d) 3

$(n-1)!$

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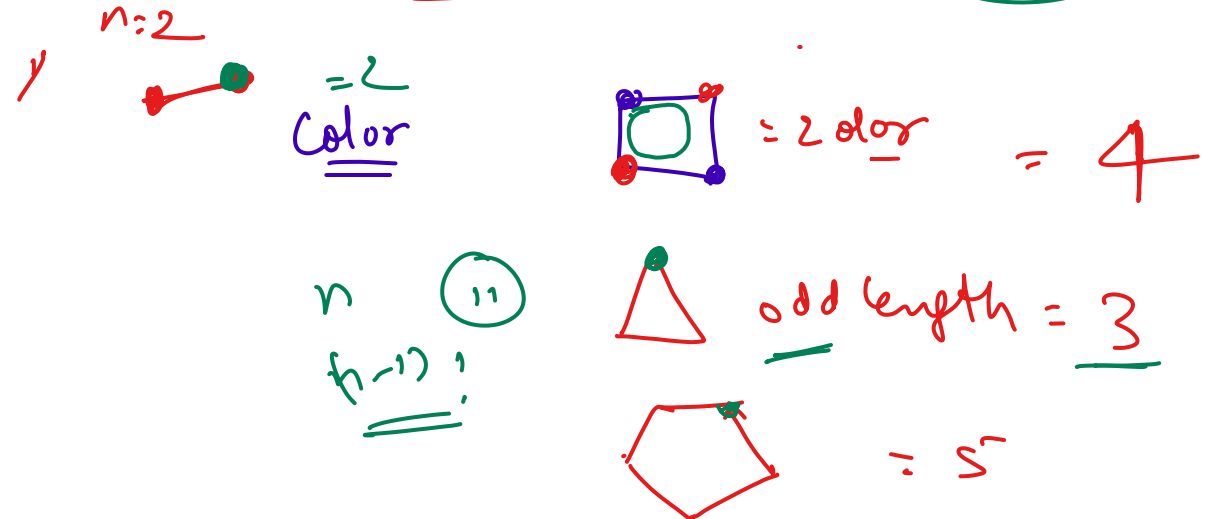


even

Q2) What is the chromatic number of n vertex simple connected graph which does not contain any odd length cycle. Assume $n \geq 2$.

$n: 1$

- a) N
- b) N-1
- c) 2
- d) 3



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Applicative Ques

Q3) Simple non-directed graph G has 24 edges & degree of each vertex is K, then which is possible no. of vertices. ==

- a) 20
- b) 15
- c) 10
- d) 8

nta

application

Q3) Simple non-directed graph G has 24 edges & degree of each vertex is K, then which is possible no. of vertices.

- theorem 2 edges
- $$\sum d(v) = 2 \times 24$$
- $n \cdot k = 48$
- $n = \frac{48}{k}$
- a) 20 $\frac{48}{20}$
 - b) 15 $\frac{48}{15}$
 - c) 10 $\frac{48}{10}$
 - d) 8 $\frac{48}{8} = 6$

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Repetitive 2018, 2019, 2020

Q4) G is undirected graph with n vertices & 25 edges such that each vertex has degree at least 3, then max possible value of n is..?

- a) 16
- b) 17

Q4) G is undirected graph with n vertices & 25 edges such that each vertex has degree at least 3, then max possible value of n is..?

- ✓ a) 16
- b) 17

3, 4, 5, ...

$$\sum \deg(v) = 2e$$
$$3n \leq 2 \times 25$$
$$n = \frac{2 \times 25}{3} = \frac{50}{3} = 16$$

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Q5) Minimum no. of vertices possible in a simple graph if 41 edges such that each vertex has degree at most 5?

a) 16

b) 17

at most 0, 1, 2, 3, 4, 5

~~20~~

$$5|V| \leq 41 \times 2$$

$$|V| \leq \frac{41 \times 2}{5}$$

$$\text{max} \leq \underline{16}$$

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Q5) Minimum no. of vertices possible in a simple graph if 41 edges such that each vertex has degree at most 5?

handshaking

a) 16

b) 17

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Tree

- Has exactly one path btw any two vertices
- not contain cycle
- connected
- No. of edges = n - 1

$$n=2$$

$$e=1$$



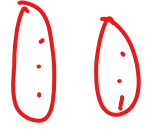
$$n=1, e=0$$

LMN

Theorem

Graph Theory

1. No. of edges in a complete graph = $n(n-1)/2$
2. Bipartite Graph : There is no edges between any two vertices of same partition.
3. In complete bipartite graph no. of edges = $m*n$
4. Bipartite graph is 2 colorable. 2020
5. Handshaking theorem - Sum of degree of all vertices is equal to twice the number of edges.
6. Maximum no. of connected components in graph with n vertices = n
7. Minimum no. of connected components
0 (null graph) , 1 (not null graph)
8. Minimum no. of edges to have connected graph with n vertices = $n-1$
9. To guarantee that a graph with n vertices is connected, minimum no. of edges required = $\{(n-1)*(n-2)/2\} + 1$
10. Euler Graph = if it there exists atmost 2 vertices of odd - degree. edge.
11. For complete graph the no. of spanning tree possible = n^{n-2}



$$\sum \text{deg}(v) = 2e$$

$$n, e=0$$

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Handshaking Theorem states in any given graph,

- Sum of degree of all the vertices is twice the number of edges contained in it.
- The sum of degree of all the vertices is always even.
- The sum of degree of all the vertices with odd degree is always even.

formula

$$\sum_{i=1}^n d(v_i) = 2 \times |E|$$

Handshaking Theorem

For Simple connected Planar graph

- A graph is planar if and only if it does not contain a subdivision of K_5 and $K_{3,3}$ as a subgraph. *2020*
- Let G be a connected planar graph, and let n, m and f denote, respectively, the numbers of vertices, edges, and faces in a plane drawing of G. Then $n - m + f = 2$. *2019*
- Let G be a connected planar simple graph with n vertices and m edges, and no triangles. Then $m \leq 2n - 4$.
- Let G be a connected planar simple graph with n vertices, where $n \geq 3$ and m edges. Then $m \leq 3n - 6$.

Planarity ↓ Graph

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